

LECTURE NOTES
ON
STRUCTURAL MECHANICS (TH. 1)
FOR
DIPLOMA IN CIVIL ENGINEERING
(3RD SEMESTER STUDENTS)
AS PER SCTE&VT SYLLABUS



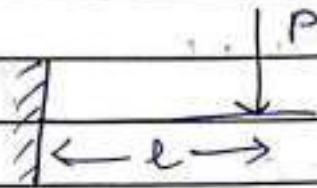
PREPARED BY:

Department of Civil Engineering
Government Polytechnic, Sambalpur (Rengali)

www.gpsambalpur.com

Moment:-

- The turning effect of the force on the body on which it is acting is measured by moment.
- It is found by multiplying the force by its distance



$$\begin{aligned}M &= P \times l \\ &= \text{N} \times \text{m} \\ &= \text{Nm} \text{ (Newton meter)}\end{aligned}$$

Conditions for Equilibrium:-

It may be defined as a state of rest or uniform motion of a body whose net force and net moment is acting upon a body is equal to zero.

⊙

Net force

Net moment

$$\sum F_x = 0$$

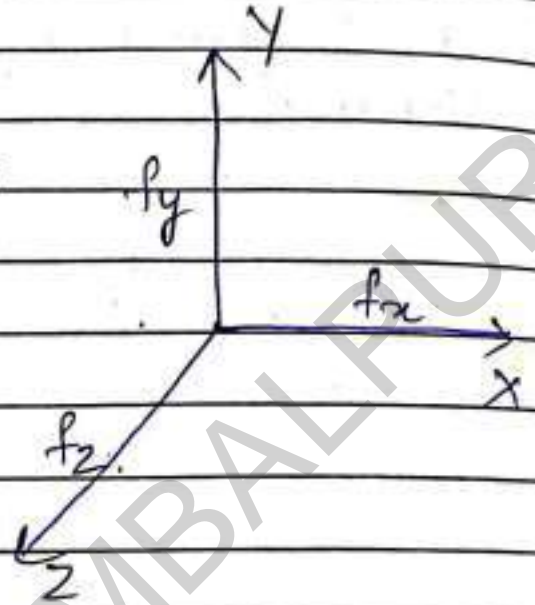
$$\sum M_x = 0$$

$$\sum F_y = 0$$

$$\sum M_y = 0$$

$$\sum F_z = 0$$

$$\sum M_z = 0$$



Net force = Net moment = zero.

Support conditions:-

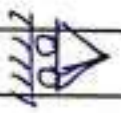
Types of supports

Represented by

Reaction force

Resisting load

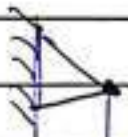
1. Roller Support



① Vertical

Vertical force

2. Pinned Support / Hinged support



② Vertical and horizontal

Vertical and horizontal

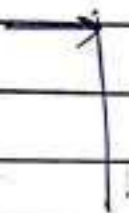
3. Fixed support



③ Vertical, horizontal, rotational

all type of loads & moment

4. Single support



④ Vertical

Vertical loads

Vertical, horizontal, rotational

Centre of gravity (C.G) :-

- Centre of gravity is an imaginary balancing point where the body weight can be assumed to be concentrated.
- Its symbol is C.G

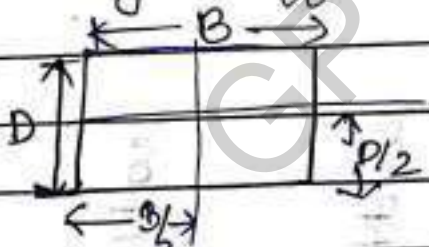
Moment of inertia (M.I) :-

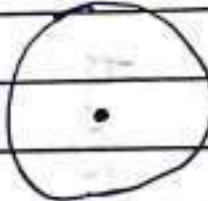
- Moment of inertia measures the resistance to a change in rotation.

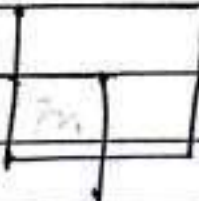
$$- \text{MI} = M \times \text{Distance}^2$$

$$= P L \times l^2$$

CG and MI of Different section.

① Rectangle		$\frac{B}{2}, \frac{D}{2}$	$\frac{BD^3}{12}$
-------------	---	----------------------------	-------------------

② circle		$\frac{D}{2}$ or r	$\frac{\pi D^4}{64}$
----------	---	----------------------	----------------------

③ Square		$\frac{a}{2}, \frac{a}{2}$	$\frac{a^4}{12}$
----------	---	----------------------------	------------------

Centre of gravity (C.G) :-

- Centre of gravity is an imaginary balancing point where the body weight can be assumed to be concentrated.
- Its symbol is \odot C.G


Moment of inertia (M.I) :-

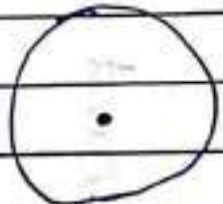
- Moment of inertia measures the resistance to a change in rotation.
- $M.I = M \times \text{Distance}^2$

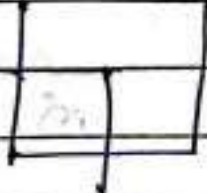
$$= P \times l^2$$

$$M = P \times l^2$$

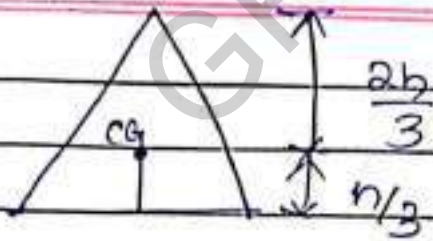
CG and MI of Different section.

① Rectangle		$\frac{B}{2}, \frac{D}{2}$	$\frac{BD^3}{12}$
-------------	---	----------------------------	-------------------

② circle		$\frac{D}{2}$ or r	$\frac{\pi D^4}{64}$
----------	---	----------------------	----------------------

③ Square		$\frac{a}{2}, \frac{a}{2}$	$\frac{a^4}{12}$
----------	---	----------------------------	------------------

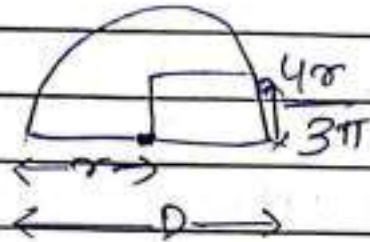
④ Triangle



$$\frac{Bb^3}{36}$$



⑤ Semicircle

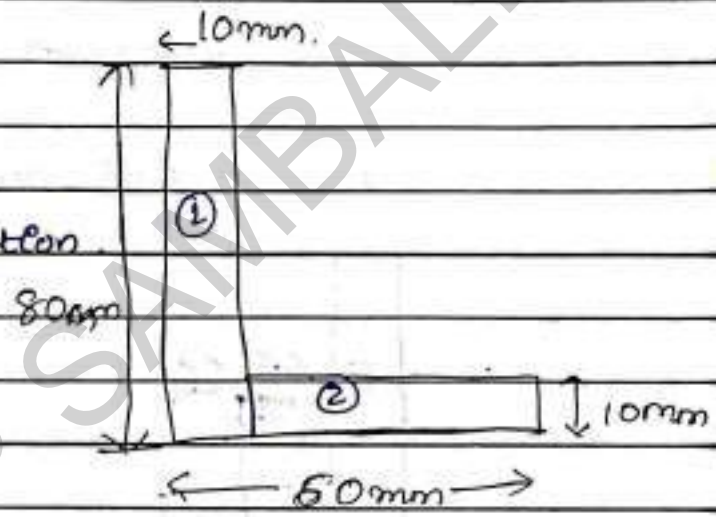


$$\frac{\pi D^4}{128}$$

Q/W
22/09/22

find the CG of given section.

Rectangle - ①



$$a_1 = 80 \times 10 = 800 \text{ mm}^2$$

$$x_1 = \frac{10}{2} = 5 \text{ mm}$$

$$y_1 = \frac{80}{2} = 40 \text{ mm}$$

Rectangle - ②

$$a_2 = 50 \times 10 = 500 \text{ mm}^2$$

$$x_2 = \frac{50}{2} = 25 \text{ mm}$$

$$y_2 = \frac{10}{2} = 5 \text{ mm}$$

$$\bar{x} = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2}$$

$$= \frac{800 \times 5 + 500 \times 25}{800 + 500}$$

$$= \frac{800 \times 5 + 500 \times 25}{800 + 500}$$

Teacher's Sign

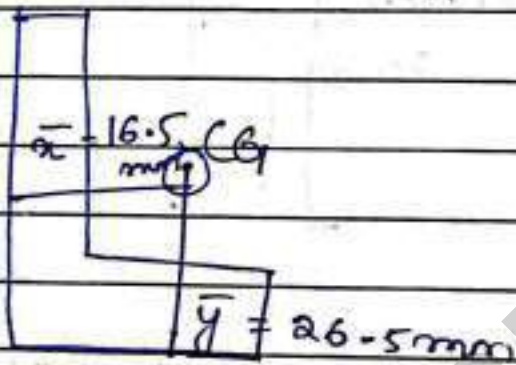
~~140~~
~~16500~~
~~12500~~
~~12500~~
16.5 mm

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$$

$$= \frac{800 \times 40 + 500 \times 5}{800 + 500}$$

$$= \frac{34500}{1300}$$

$$= 26.5 \text{ mm}$$

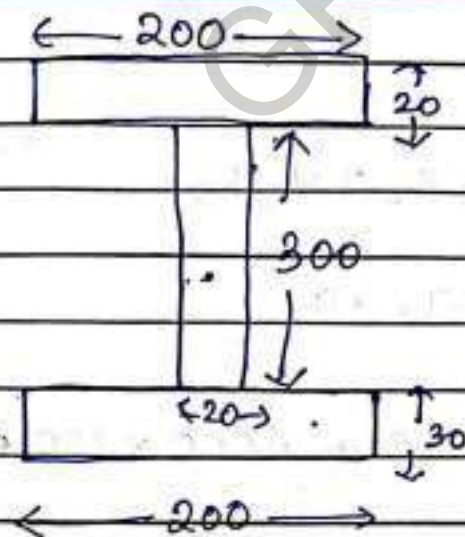


Q Find the CG of a T-section for the given data.

Top flange :- 200×20

web :- 300×20

Bottom flange :- 200×30



Bottom flange

web

$$a_1 = 200 \times 30$$

$$= 6000 \text{ mm}^2$$

$$a_2 = 300 \times 20$$

$$= 6000 \text{ mm}^2$$

$$x_1 = \frac{200}{2}$$

$$= 100 \text{ mm}$$

$$x_2 = \frac{20}{2} + 30$$

$$= 10 + 30$$

$$= 40 \text{ mm}$$

$$y_1 = \frac{30}{2}$$

$$= 15 \text{ mm}$$

$$y_2 = 100 + 100$$

$$= 200 \text{ mm}$$

$$\text{web} \rightarrow a_3 = 200 \times 20$$

$$= 4000 \text{ mm}^2$$

$$y_2 = 30 + \frac{300}{2}$$

$$= 30 + 150$$

$$= 180 \text{ mm}$$

$$x_3 = \frac{200}{2} = 100 \text{ mm}$$

$$y_3 = \frac{300 + 30 + 20}{2}$$

$$= 175 \text{ mm}$$

$$\bar{x} = \frac{a_1 x_1 + a_2 x_2 + a_3 x_3}{a_1 + a_2 + a_3}$$

$$= \frac{6000 \times 100 + 6000 \times 100 + 4000 \times 100}{6000 + 6000 + 4000}$$

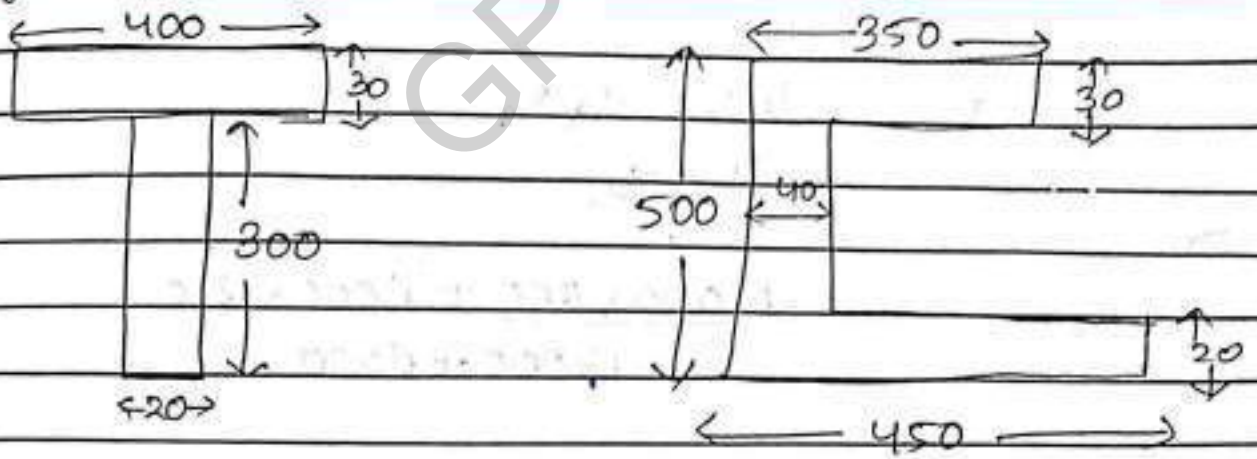
$$= 100 \text{ mm}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2 + a_3 y_3}{a_1 + a_2 + a_3}$$

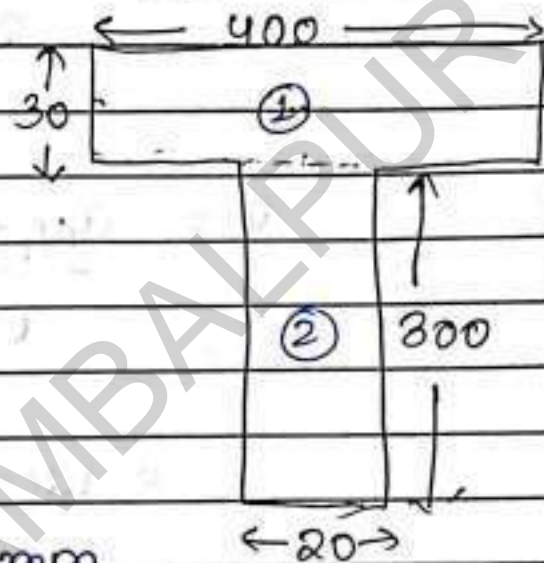
$$= \frac{6000 \times 15 + 6000 \times 180 + 4000 \times 340}{6000 + 6000 + 4000}$$

$$= 158.2 \text{ mm}$$

Assignment:-



Q1



Rectangle - ①

$$\text{area } (a_1) = 400 \times 30 \\ = 12000 \text{ mm}^2.$$

$$x_1 = \text{200mm} \quad 190 + 10 = 200 \text{ mm}$$

$$y_1 = 300 + \frac{30}{2} = 300 + 15 = 315 \text{ mm}$$

Rectangle - ②

$$\text{area } (a_2) = 300 \times 20 \\ = 6000 \text{ mm}^2.$$

$$x_2 = 200 \text{ mm.}$$

$$y_2 = \frac{300}{2} = 150 \text{ mm}$$

$$\bar{x} = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2}$$

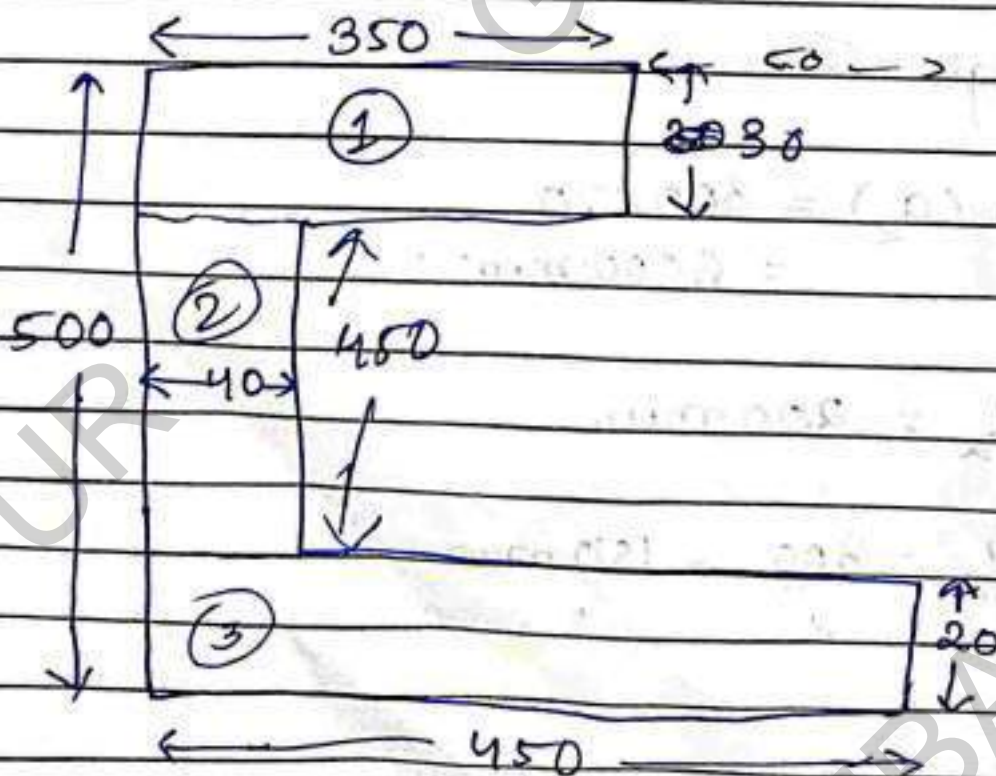
$$= \frac{12000 \times 200 + 6000 \times 200}{12000 + 6000}$$

$$= 200 \text{ mm}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$$

$$= \frac{12000 \times 315 + 6000 \times 150}{12000 + 6000}$$

$$= 260 \text{ mm}$$



Rectangle - (1)

$$\text{area} = 350 \times 30$$

$$(a_1) = 10500 \text{ mm}^2.$$

$$x_1 = \frac{350}{2}$$

$$= 175 \text{ mm}$$

$$y_1 = \frac{20 + 450 + 30}{2}$$

$$= \frac{20 + 450 + 15}{2}$$

$$= 485 \text{ mm}$$

Rectangle - (2)

$$\text{area} = 450 \times 40$$

$$(a_2) = 18000 \text{ mm}^2.$$

$$x_2 = \frac{40}{2} = 20 \text{ mm}$$

$$y_2 = \frac{20 + 450}{2}$$

$$= 245 \text{ mm}$$

Rectangle - (3)

$$\text{area} = 450 \times 20$$

$$(a_3) = 9000 \text{ mm}^2.$$

$$x_3 = \frac{450}{2} = 225 \text{ mm}$$

$$y_3 = \frac{20}{2} = 10 \text{ mm}$$

$$\bar{x} = \frac{10500 \times 175 + 18000 \times 20 + 9000 \times 225}{10500 + 18000 + 9000}$$

$$= 112.6 \text{ mm}$$

$$\bar{y} = \frac{10500 \times 485 + 18000 \times 245 + 9000 \times 10}{10500 + 18000 + 9000}$$

$$= 255.8 \text{ mm}$$

Moment of inertia

Rect 1

MI of Rectangle ① :-

$$I_{xx_1} = I_x + A e^2$$

$$= \frac{350 \times 30^3}{12} + 10500 \times 485^2$$

$$= 2.47 \times 10^9 \text{ mm}^4$$

MI of Rectangle ②

$$I_{xx_2} = I_x + A e^2$$

$$= \frac{40 \times 450^3}{12} + 18000 \times 245^2$$

$$= 1.38 \times 10^9 \text{ mm}^4$$

MI of Rectangle ③

$$I_{xx_3} = I_x + Al^2.$$

$$= \frac{450 \times 20^3}{12} + 9000 \times 30^2$$

$$= 1.2 \times 10^6 \text{ mm}^4$$

$$I_{xx} = I_{xx_1} + I_{xx_2} + I_{xx_3}$$

$$= (2.47 \times 10^9 + 1.39 \times 10^9 + 1.2 \times 10^6) \text{ mm}^4$$

$$= 3.86 \times 10^9 \text{ mm}^4$$

(Ans)

$$I_{yy} = (I_{y_1} + Al^2) + (I_{y_2} + Al^2) + (I_{y_3} + Al^2)$$

~~Rec-1~~

$$\text{Rec-①} = I_{y_1} + Al^2$$

$$= \frac{30 \times 350^3}{12} + 10500 \times 175^2$$

$$= \cancel{409.02 \times 10^6 \text{ mm}^4} \quad 428.75 \times 10^6 \text{ mm}^4$$

$$\text{Rec-②} = I_{y_2} + Al^2$$

$$= \frac{450 \times 40^3}{12} + 18000 \times 20^2$$

12

$$= 9.6 \times 10^6 \text{ mm}^4$$

Rectangle - (3)

$$\begin{aligned} I_{x_3} &= I_{x_1} + A_1^2 \\ &= \frac{20 \times 450^3}{12} + 9000 \times 225^2 \\ &= 607.5 \times 10^6 \text{ mm} \end{aligned}$$

$$\begin{aligned} I_{yy} &= I_{y_1} + I_{y_2} + I_{y_3} \\ &= 428.75 \times 10^6 + 9.6 \times 10^6 + 607.5 \times 10^6 \text{ mm} \\ &= 1.04 \times 10^9 \text{ mm} \end{aligned}$$

Q1) Find the CG of the T-section with flange 150 mm x 850 and web as 150 x 50 mm. [5]

Q2) Find the CG of an T-section for the given data [5]

Data:-

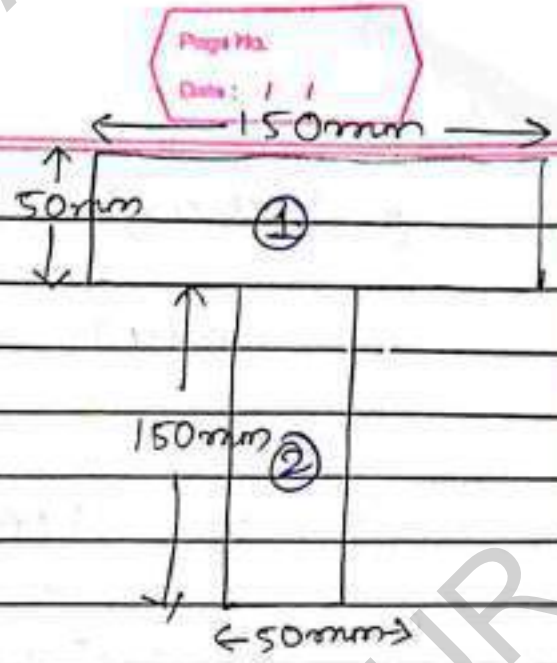
Top flange = 300 x 30 mm

Bottom flange = 200 x 20 mm

web = 350 x 10 mm

Assignment

Rectangle - (1)



$$\text{Area } (a_1) = (150 \times 50) \text{ mm}^2 \\ = 7500 \text{ mm}^2$$

$$x_1 = \frac{150}{2} = 75 \text{ mm}$$

$$y_1 = 150 + \frac{50}{2} \\ = 150 + 25 \\ = 175 \text{ mm}$$

Rectangle - (2)

$$\text{Area } (a_2) = 150 \times 50 \text{ mm}^2 \\ = 7500 \text{ mm}^2$$

$$x_2 = 50 + 25 = 75 \text{ mm}$$

$$y_2 = \frac{150}{2} = 75 \text{ mm}$$

$$\bar{x} = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2}$$

$$= \frac{7500 \times 75 + 7500 \times 75}{7500 + 7500}$$

$$= 75 \text{ mm}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$$

$$= \frac{7500 \times 175 + 7500 \times 75}{7500 + 7500}$$

$$= 125 \text{ mm}$$

Q2 Rectangle - (1)

$$\text{area } (a_1) = 300 \times 30 \\ = 9000 \text{ mm}^2.$$

$$x_1 = \frac{300}{2} = 150 \text{ mm}$$

$$y_1 = 20 + 350 + 15 = 385 \text{ mm}$$

Rectangle - (2)

$$\text{area } (a_2) = 350 \times 10 \\ = 3500 \text{ mm}^2.$$

$$x_2 = 150 \text{ mm}$$

$$y_2 = 20 + \frac{350}{2}$$

$$= 20 + 175$$

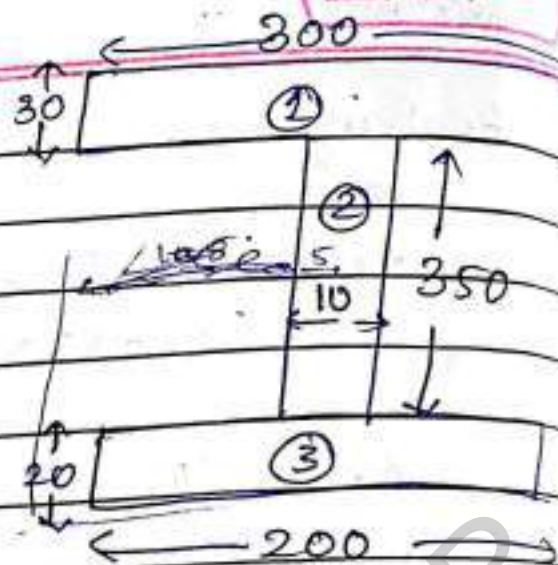
$$= 195 \text{ mm}$$

Rectangle - (3)

$$\text{area } (a_3) = 200 \times 20 = 4000 \text{ mm}^2.$$

$$x_3 = \frac{200}{2} = 100 \text{ mm}$$

$$y_3 = \frac{20}{2} = 10 \text{ mm}$$



$$\bar{x} = \frac{a_1x_1 + a_2x_2 + a_3x_3}{a_1 + a_2 + a_3}$$

$$= \frac{9000 \times 150 + 3500 \times 150 + 4000 \times 150}{9000 + 3500 + 4000}$$

$$= 150 \text{ mm}$$

$$\bar{y} = \frac{a_1y_1 + a_2y_2 + a_3y_3}{a_1 + a_2 + a_3}$$

$$= \frac{9000 \times 385 + 3500 \times 195 + 4000 \times 10}{9000 + 3500 + 4000}$$

$$= 253.78 \text{ mm}$$

Assign. MI of T section

From Rectangle-①

$$\begin{aligned} \text{Area } (a_1) &= 400 \times 30 \\ &= 12000 \text{ mm}^2. \end{aligned}$$

$$\begin{aligned} y_1 &= 300 + 15 \\ &= 315 \text{ mm} \end{aligned}$$



Rectangle-②

$$\begin{aligned} \text{Area } (a_2) &= 300 \times 20 \\ &= 6000 \text{ mm}^2. \end{aligned}$$

$$\begin{aligned} y_2 &= \frac{300}{2} \\ &= 150 \text{ mm} \end{aligned}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$$

$$= \frac{12000 \times 315 + 6000 \times 150}{12000 + 6000}$$

$$= 260 \text{ mm}$$

MI of Rectangle - (1)

$$I_{xx_1} = I_x + Al^2$$

$$= \frac{400 \times 30^3}{12} + 12000 \times (315 - 260)^2$$

$$= \cancel{1.56 \times 10^6 \text{ mm}^4} \quad 37.2 \times 10^6$$

MI of Rectangle - (2)

$$I_{xx_2} = I_x + Al^2$$

$$= \frac{20 \times 300^3}{12} + 6000 \times (260 - 150)^2$$

$$= \cancel{45.66 \times 10^6 \text{ mm}^4} \quad 117.6 \times 10^6$$

$$I_{xx} = I_{xx_1} + I_{xx_2}$$

$$= 1.56 \times 10^6 + 45.66 \times 10^6$$

$$= 47.22 \times 10^6 \text{ mm}^4$$

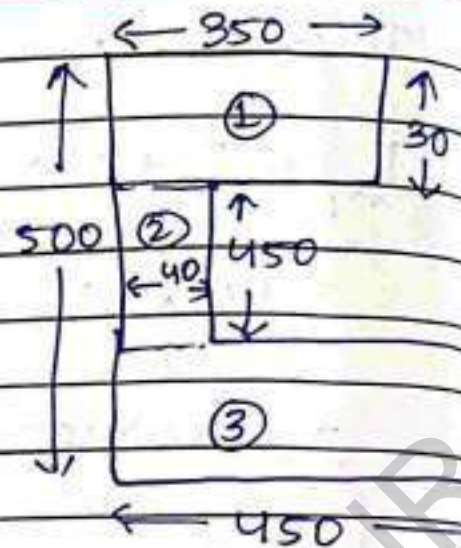
MI of C-section:

Rectangle - ①

$$\text{area}(a_1) = 350 \times 30 \\ = 10500 \text{ mm}^2.$$

$$x_1 = \frac{350}{2} = 175 \text{ mm}$$

$$y_1 = 20 + 450 + \frac{30}{2} \\ = 485 \text{ mm}$$



Rectangle - ②

$$\text{area}(a_2) = 450 \times 40 \\ = 18000 \text{ mm}^2.$$

$$x_2 = \frac{40}{2} = 20 \text{ mm}$$

$$y_2 = 20 + \frac{450}{2} \\ = 245 \text{ mm}$$

Rectangle - ③

$$\text{area}(a_3) = 450 \times 20 \\ = 9000 \text{ mm}^2$$

$$x_3 = 225 \text{ mm}$$

$$y_3 = 10 \text{ mm}$$

$$\bar{x} = \frac{a_1 x_1 + a_2 x_2 + a_3 x_3}{a_1 + a_2 + a_3}$$

$$= \frac{10500 \times 175 + 18000 \times 20 + 9000 \times 225}{10500 + 18000 + 9000}$$

$$= 112.6 \text{ mm}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2 + a_3 y_3}{a_1 + a_2 + a_3}$$

$$= \frac{10500 \times 485 + 18000 \times 245 + 9000 \times 10}{10500 + 18000 + 9000}$$

$$= 255.8 \text{ mm}$$

$$I_{xx1} = I_x + A l^2$$

$$= \frac{350 \times 30^3}{12} + 10500 \times \cancel{225^2} (485 - 255.8)^2$$

$$= \cancel{3219 \times 10^6 \text{ mm}^4} \cdot 552.38 \times 10^6 \text{ mm}^4$$

$$I_{xx2} = I_x + A l^2$$

$$= \frac{40 \times 45^3}{12} + 18000 \times (255.8 - 245)^2$$

$$= \cancel{3087.84 \times 10^6 \text{ mm}^4}$$

$$= 305.84 \times 10^6 \text{ mm}^4$$

$$I_{xx_3} = I_{x_3} + A_3 l^2$$

$$= \frac{450 \times 20^3}{12} + 9000 \times (255.8 - 10)^2$$

$$= 544.05 \times 10^6 \text{ mm}^4$$

$$I_{xx} = I_{xx_1} + I_{xx_2} + I_{xx_3}$$

$$= 552.38 \times 10^6 + 308.84 \times 10^6 + 544.05 \times 10^6$$

$$= 1.402 \times 10^9 \text{ mm}^4$$

$$I_{yy_1} = I_{y_1} + A_1 l^2$$

$$= \frac{30 \times 350^3}{12} + 10500 \times (175 - 112.6)^2$$

$$= 148.07 \times 10^6 \text{ mm}^4$$

$$I_{yy_2} = I_{y_2} + A_2 l^2$$

$$= \frac{450 \times 40^3}{12} + 18000 \times (112.6 - 20)^2$$

$$= 156.74 \times 10^6 \text{ mm}^4$$

$$I_{yy_3} = I_{y_3} + A_3 l^2$$

$$= \frac{20 \times 450^3}{12} + 9000 \times (225 - 112.6)^2$$

$$= 265.57 \times 10^6 \text{ mm}^4$$

$$\begin{aligned}
 I_{yy} &= I_{yy_1} + I_{xx_2} + I_{xx_3} \\
 &= (148.07 \times 10^6 + 156.74 \times 10^6 + 265.07 \times 10^6) \text{ mm}^4 \\
 &= 570.38 \times 10^6 \text{ mm}^4.
 \end{aligned}$$

MI of Rectangle - ① $I_{xx_1} = I_x + A d^2$.

Assign

$$= \frac{150 \times 50^3}{12} + 7500 \times (175 - 125)^2$$

$$= 20.31 \times 10^6 \text{ mm}^4.$$

Rec - ② $I_{xx_2} = I_x + A d^2$.

$$= \frac{50 \times 150^3}{12} + 7500 \times (125 - 75)^2$$

$$= 32.81 \times 10^6 \text{ mm}^4.$$

$$I_{xx} = I_{xx_1} + I_{xx_2}$$

$$= 20.31 \times 10^6 + 32.81 \times 10^6 \text{ mm}^4$$

$$= 53.12 \times 10^6 \text{ mm}^4$$

$$I_{yy_1} = I_{y_1} + A_1^2$$

$$= \frac{50 \times 150^3}{12} + 7500 \times \cancel{(150 - 150)^2} \cdot (25 - 25)$$

$$= 14.06 \times 10^6 \text{ mm}^4$$

$$I_{yy_2} = I_{y_2} + A_1^2$$

$$= \frac{150 \times 50^3}{12} + 7500 (0)^2$$

$$= 1.56 \times 10^6 \text{ mm}^4$$

$$I_{yy} = I_{yy_1} + I_{yy_2}$$

$$= 14.06 \times 10^6 + 1.56 \times 10^6 \text{ mm}^4$$

$$= 15.62 \times 10^6 \text{ mm}^4$$

I-section

Page No.

Date: / /

MI of Rectangle - (1)

$$I_{xx} = I_{x_{18}} + Ae^2.$$

$$= \frac{300 \times 30^3}{12} + 9000 \times (253.78 - 385 - 253.78)^2$$

$$= 155.64 \times 10^6 \text{ mm}^4.$$

$$I_{xx_2} = I_{x_2} + Ae^2.$$

$$= \frac{10 \times 350^3}{12} + 3500 \times (253.78 - 195)^2$$

$$= 47.82 \times 10^6 \text{ mm}^4$$

$$I_{xx_3} = I_{x_3} + Ae^2.$$

$$= \frac{200 \times 20^3}{12} + 4000 \times (253.78 - 10)^2$$

$$= 237.84 \times 10^6 \text{ mm}^4.$$

$$I_{xx} = I_{xx_1} + I_{xx_2} + I_{xx_3}$$

$$= 155.64 \times 10^6 + 47.82 \times 10^6 + 15.62 \times 10^6$$

$$= 219.08 \times 10^6 \text{ mm}^4$$

Columns & Struts

Struts:- A member or structure or bar which carries an axial compressive load is known as Struts.

Columns:- If the Struts is vertical i.e., at 90° to the horizontal, is known as column.

→ All columns are struts but all struts are not columns.

Difference between ~~crushing~~ ^{crushing} and buckling:-

Crushing

Buckling

(i) It is applicable to short column only.

(i) It is applicable to long column only.

(ii) Stress = $\frac{P}{A}$
Unit = N/m².

(ii)
$$P_e = \frac{\pi^2 EI}{l_e^2}$$

where P_e = Euler's load

I = moment of inertia


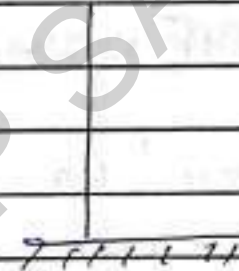
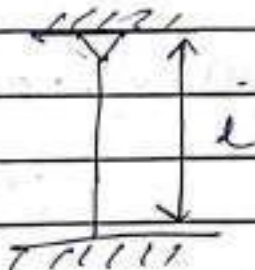
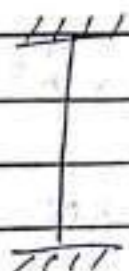
E = young's modulus of elasticity

l_e = Effective length

Young's modulus of Elasticity :- (E)

The material which has ability to return its original shape after removing the load is known as elasticity

Effective length of column :- (l_e)

Sl No.	column condition	figure	Effective length (l_e)
1.	Both ends are Hinged/pinned		$l_e = l$
2.	One end fixed and other end free		$l_e = 2l$
3.	one end is fixed and another end is hinged		$l_e = \frac{l}{\sqrt{2}}$
4.	Both ends are fixed		$l_e = \frac{l}{2}$

Q A steel rod is 5m long and 850mm diameter is used as column with one end fixed and other free. Determine the Buckling load by using Euler's formula. Take $E = 200 \text{ GPa}$.

$$E = 200 \text{ GPa}$$

$$I = \frac{\pi d^4}{64}$$

$$= \frac{3.14 \times (50 \times 10^{-3})^4}{64}$$

$$= \frac{3.14 \times (0.05)^4}{64}$$



$$l_e = 2l$$

$$= 2 \times 5$$

$$= 10 \text{ m}$$

$$I = \frac{3.14 \times (0.05)^4}{64} = 3.06 \times 10^{-7} \text{ m}^4$$

$$E = 200 \times 10^9 \text{ Pa}$$

$$P_e = \frac{(3.14)^2 \times 200 \times 10^9 \times 3.06 \times 10^{-7}}{(10)^2}$$

$$= \frac{6.03 \times 10^{15}}{10^4}$$

$$= 6.03 \times 10^3$$

$$P_e = 6.03 \text{ kN}$$

$$1 \text{ Pa} = 1 \text{ N/m}^2.$$

$$1 \text{ KPa} = 10^3 \text{ N/m}^2.$$

$$1 \text{ MPa} = 10^6 \text{ N/m}^2$$

$$1 \text{ GPa} = 10^9 \text{ N/m}^2.$$

Q2 A steel rod of 60mm diameter and 15m length is used as column. Determine the buckling load by using Euler's formula. Take $E = 250 \text{ GPa}$

(i) Both ends are fixed

(ii) ~~Both~~ one end is fixed and ^{an} other end is hinged

$$E = 250 \text{ GPa} \\ = 250 \times 10^9 \text{ N/m}^2.$$

$$I = \frac{\pi d^4}{64} = \frac{3.14 \times (0.06)^4}{64}$$

$$= \frac{3.14 \times 1.296 \times 10^{-4}}{64} = 6.35 \times 10^{-7} \text{ m}^4.$$

$$L_e = \frac{L}{2} = \frac{15}{2} = 7.5 \text{ m}$$

$$P_e = \frac{\pi^2 EI}{L_e^2}$$

$$= \frac{(3.14)^2 \times 250 \times 10^9 \times 6.35 \times 10^{-7}}{(7.5)^2}$$

$$= \frac{771 \times 10^6 \text{ N}}{56.25} = 27.85 \text{ kN}$$

$$E = 250 \text{ GPa}$$

$$= 250 \times 10^9 \text{ N/m}^2.$$

$$I = \frac{\pi d^4}{64}$$

$$= \frac{3.14 \times (0.06)^4}{64}$$

$$= \cancel{1.76 \times 10^{-4} \text{ mm}^4} \cdot 6.35 \times 10^{-7}.$$

$$l_e = \frac{15}{\sqrt{2}}$$

$$= 10.60 \text{ m}$$

$$P_e = \frac{\pi^2 EI}{l_e^2}$$

$$= \frac{(3.14)^2 \times 250 \times 10^9 \times 1.76 \times 10^{-4}}{(10.60)^2}$$

$$= \cancel{4.28 \times 10^6 \text{ N}}$$

$$= 15.48 \text{ kN}.$$

Assumptions made in Euler's Formula:- [5 M]

- 1) - Material should be elastic, isotropic & homogeneous.
- 2) - The column should be perfectly straight and uniform.
- 3) - Load is applied axially and passes through the centroid.
- 4) - This is valid for long columns only.

Slenderness ratio:- [2 Mark]

- The ratio of Effective length to minimum Radius of Gyration is called Slenderness ratio.

$$SR = \frac{\text{Effective length } (l_e)}{\text{Min}^m \text{ Radius of gyration}}$$

$$\boxed{SR = \frac{l_e}{k}}$$

Minimum Radius of Gyration:- [2 M]

It may be defined as the square ^{root} of the ratio of moment of inertia of a body to its cross-sectional area.

**

$$K = \frac{I}{\sqrt{A}}$$

It is unitless

$$SR = \frac{le}{\sqrt{\frac{BD^3}{12}}}$$

$$= \frac{le}{\sqrt{\frac{BD^3}{12} \times \frac{1}{BD}}}$$
$$= \frac{le}{\sqrt{12} \cdot D}$$

SHORT COLUMN and Long column:-

(1) Short column:- Columns having their length ~~less~~ < 8 times of their respective diameter or Slenderness ratio < 32 are known as Short column.

(2) Long column:- The columns having their length greater than 30 times of the diameter or Slenderness ratio greater than 120 are known as long column.

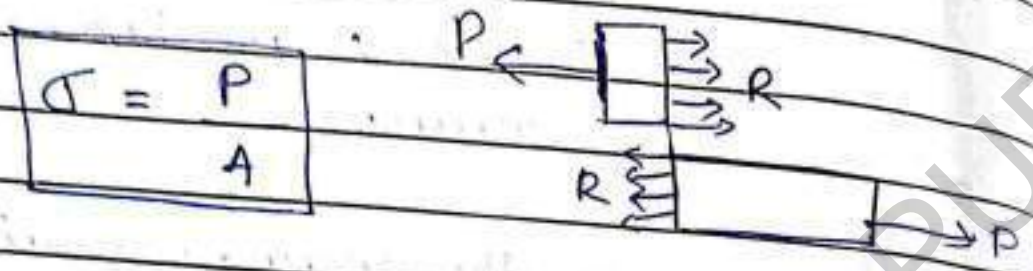
Between < 32 and > 120 is known as Intermediate column.

2 Marks

Simple Stresses and Strains

Page No. 11

Stress - It is the resistance offered by a body against the deformation is known as stress.



It is denoted by the symbol Sigma (σ)

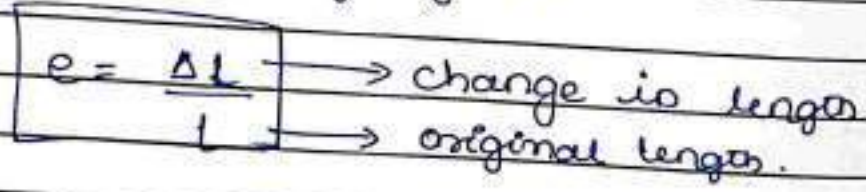
where P = Force or Load

A = Cross-sectional area

unit of stress - N/m^2

Strains :- It is the ratio of change in dimension to original dimension

- It is denoted by symbol 'e'



It is a unitless quantity



Teacher's Signature.....